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BASIC DIGITAL LOGIC COURSE

PART I: NUMBER SYSTEMS

THE emergence of experimental digital IC projects has been so rapid that many people tend to get lost amid strange-sounding names like "quad 2-input positive NAND gate" and "BCD to 7-segment decoder/driver." Such terms describe the building blocks of digital electronics. To provide an introduction to logic for beginners and refresher information for more advanced experimenters, here is the beginning of a Digital Logic Course series.

This first instalment describes number systems and provides important background information for the next two instalments.

Number Systems. Early man was forced to count with small pebbles or knots on a string when he wanted to inventory his possessions. As time went on, and perhaps because he found it convenient to count with his fingers, man eventually devised a number system with ten digits. This provided a far more convenient and versatile counting system since, for

example, the number 16 could be represented with merely two digits rather than 16 pebbles or knots.

The comparatively recent development of electronic digital computers has revived interest in number systems based on something besides the decimal. A system based on two digits is of particular importance in electronic digital computers. The reason for this is that an electronic circuit can be made to occupy only one of two states: on or off (saturated or cut off). Of equal significance is that any form of logic statement can be reduced to contain only true and false assertions.

Since electronic circuits required to implement true and false logic statements are very simple, a computer can be designed based on a two-digit number system, in which one digit corresponds to "true" and the other to "false". The two-digit, or base-two, number system is called the binary system and its digits, called bits (for *binary* digits), are 1 and 0.

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The Binary System. The easiest way to understand the binary system is to learn to count in binary fashion. One basic rule governs counting in any number system: record successive digits for each count until the count exceeds the total number of available digits; then start a second column to the left of the first and resume counting.

Since the binary system has only two digits, counting is very easy. You can prove this to yourself by counting to the equivalent of the decimal number 10 in binary. The binary of decimal 0 is 0. The binary of 1 is 1. Here the similarity ends. To express 2 in binary, you must start a new column since both binary, bits have been used in the first column. Hence, the binary of 2 is 10 (read one-zero—not ten). Three is expressed as 11 (one-one) in binary, which uses up both binary bits for the first two columns. So, a new column must be started for binary 4, which becomes 100, while 5, 6, and 7 become 101, 110, and 111. With 8, represented by the binary 1000, we must once again start a new column.

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Binary Arithmetic. By learning how to count in binary, we have also derived three basic rules for addition: (1) $0 + 0 = 0$; (2) $0 + 1 = 1$; and (3) $1 + 1 = 10$ (1 + 1 = 0, carry 1). These rules can be used to add any two binary numbers. For example, let us add 12 and 9 in binary:

$$\begin{array}{r} 1100 \\ +1001 \\ \hline \end{array}$$

Start with the right-hand column and add the *least* significant digit. Then continue adding each successive column, working from right to left, finishing up with the *most* significant bit:

$$\begin{array}{r} 1100 \\ +1001 \\ \hline 10101 \end{array}$$

Note in the above example that the addition of the two most significant bits yielded a 0 with a 1 carry. A carry can also occur within the addition as in: $1011 + 1101 = 11000$.

Converting Binary to Decimal. Binary numbers are fundamentally easy to work with. But how do you convert a string of 1's and 0's to easily recognized decimal numbers? The process is simple, using a technique known as "expansion." Each digit column of a decimal number corresponds to a power of the base-10 to which it must be raised. Let us use the number 846 as an example:

$$\begin{array}{r} 10^2 \quad 10^1 \quad 10^0 \\ 8 \quad 4 \quad 6 \\ \hline 8 \times 10^2 = 800 \\ 4 \times 10^1 = 40 \text{ (add)} \\ 6 \times 10^0 = 6 \\ \hline 846 \end{array}$$

A binary number can be expanded in the same way and converted into a decimal number. For example, let us expand $(10111)_2$. The subscript denotes the base of the number system—in this case, 2 or "binary"—and helps in preventing confusion. The expansion is as follows:

$$\begin{array}{r} 2^4 \quad 2^3 \quad 2^2 \quad 2^1 \quad 2^0 \\ 1 \quad 0 \quad 1 \quad 1 \quad 1 \\ \hline 1 \times 2^4 = 16 \\ 0 \times 2^3 = 0 \\ 1 \times 2^2 = 4 \text{ (add)} \\ 1 \times 2^1 = 2 \\ 1 \times 2^0 = 1 \\ \hline (23)_{10} \end{array}$$

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Since the position of each digit in a binary number determines the power of 2 invoked, it is easy to convert binary to decimal simply by assigning the decimal equivalent to each column. A 0 in a column means that the column's power-of-2 decimal equivalent is *not* invoked. Therefore, the decimal equivalents of all columns containing a 1 are added to find the total decimal equivalent. Let us convert 10011 to decimal:

$$\begin{array}{r} 16 \quad 8 \quad 4 \quad 2 \quad 1 \\ 1 \quad 0 \quad 0 \quad 1 \quad 1 \\ \hline 16 + 0 + 0 + 2 + 1 = (19)_{10} \end{array}$$

Manual binary arithmetic involving numbers containing more than three or four bits is both tedious and cumbersome when you are accustomed to counting in a decimal system. But an electronic computer can perform thousands of lengthy binary additions in fractions of a second. This ability is vital to the success of digital computers and calculators, since all arithmetic operations can be performed by addition or its variations. Subtraction is the inverse of addition, while multiplication is simply repeated additions and division is the inverse of multiplication.

These facts about addition are important because they mean that even the most complicated arithmetic operations can be solved by addition. In practice, manual arithmetic rarely invokes this process. After all, you would find it inconvenient to multiply 641 by 197 if you had to write 197 times the number 641 and add the columns. But an electronic computer does the equivalent of this in only a few milliseconds.

The Octal System. Sometimes binary numbers are condensed into other number systems to further simplify computer processing. Since the binary system has only two digits, it does not take long to accumulate a string of seemingly endless 1's and 0's. A decimal number with only two digits, for example, requires five binary bits. A six-digit decimal number requires 19 bits.

Complicated binary numbers can be simplified by dividing them into groups of three or four bits and encoding the results in other number systems. Since the binary numbers for the decimal dig-

its 0 through 7 form groups of no more than three binary digits each, a long binary number can be reduced to a third of its length by converting it to a base-8, or *octal*, number system.

You can use a table of octal numbers and their binary equivalents to convert a long binary number such as 11101100001101 into octal. First, divide the number into groups of three bits each, beginning with the least significant bit:

11 101 100 001 101.

Then assign the octal equivalent to each three-bit group, using the octal-

Decimal	Binary	Octal
0	0	0
1	1	1
2	10	2
3	11	3
4	100	4
5	101	5
6	110	6
7	111	7
8	1000	10
9	1001	11
10	1010	12
11	1011	13
12	1100	14
13	1101	15
14	1110	16
15	1111	17
16	10000	20
17	10001	21
18	10010	22
19	10011	23
20	10100	24

to-binary equivalents given in the table:

11 101 100 001 101
3 5 4 1 5

Hence, $(11101100001101)_2$ equals $(35415)_8$. It is obvious that the latter number is easier to process than the former.

Sometimes the base-16 (*hexadecimal*) number system is used to further simplify long binary numbers. The hexadecimal technique requires that the binary number be subdivided into groups of four bits each, again starting with the least significant digit. The result is a hexadecimal number that is only a fourth the length of the original binary number.

Next month, we will discuss logic concepts and circuits and demonstrate how logic circuits can be combined to make a binary adder.

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